# Bigelow-Albatross Calibration for Skate Complex

Skate Plan Development Team

#### Beta-Binomial Model

 Binomial model at each station for number captured by Bigelow conditional on number captured by Both (Bigelow + Albatross)

$$N_{Bi}(L) \square Bin(N_i(L), p_i(L))$$

 Probability parameter is random across stations according to beta distribution

$$p_i(L) \square Beta(\pi(L), \phi(L))$$

### Mean Model from CRD 10-05 (Model 1)

$$\log\left(\frac{\pi}{1-\pi}\right) = \log(\rho)$$

- $\pi$  is the (mean) probability of capture by the Bigelow
- $\rho = E(C_B)/E(C_A)$  is the calibration factor

#### Length Models (2 and 3)

$$\log\left(\frac{\pi(L)}{1-\pi(L)}\right) = \log\left[\rho(L)\right] + \log\left(SA_B / SA_A\right) + \log\left(SF_B / SF_A\right)$$

- $\bullet \pi(L)$  is the (mean) probability of capture by the Bigelow
- ullet 
  ho(L) is the relative catch efficiency (B/A)
- SA is the swept area
- SF is the sampling fraction
- Based on  $E(C) = q \times SA \times D$

#### Dispersion Models (2 and 3)

For orthogonal polynomial and penalized smoothers,

$$\log[\phi(L)] = \alpha_1 \log(SA_B / SA_A) + \alpha_2 \log(SF_B / SF_A) + \varphi(L)$$

• For the gamma-based beta-binomial model,

$$\log[\phi(L)] = \log[SF_ASA_A + \rho(L)SF_BSA_B] + \varphi(L)$$

#### Smoothers for Length Models (2 and 3)

$$\log[\rho(L)] = \sum_{i=0}^{D} \beta_i g_i(L) \qquad \varphi(L) = \sum_{i=0}^{D} \beta_i g_i(L)$$

- The more terms, the less smooth the fit can be.
- For orthogonal polynomial, D is the degree of the polynomial and  $g_i(L)$  are uncorrelated
  - $-\ D$  ranges from 0 to 12 for both relative catch efficiency and dispersion parameter
- For penalized smoothers  $g_i(L)$  are basis components and D is the number of columns of the basis
  - The number parameters is estimated via a penalty term.

#### Season and Region (Model 3)

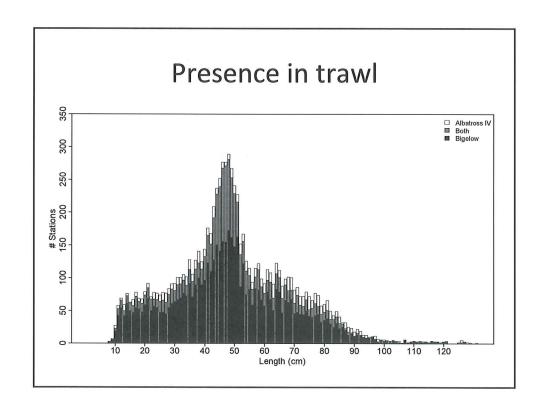
- "Season" is whether the data were obtained during the spring or fall surveys or during non-survey tows conducted during summer and fall (site-specific).
- Models accounting for season estimated parameters specific to each season
- North and South Regions were defined: North side of Georges Bank and Gulf of Maine or everything below
- Strata are given in Table 4
- Models accounting for region also accounted for season.
- Estimated parameters were region and season specific
- We intended to further consider depth categories (Table 5) but data were insufficient for some season/region/depth subsets

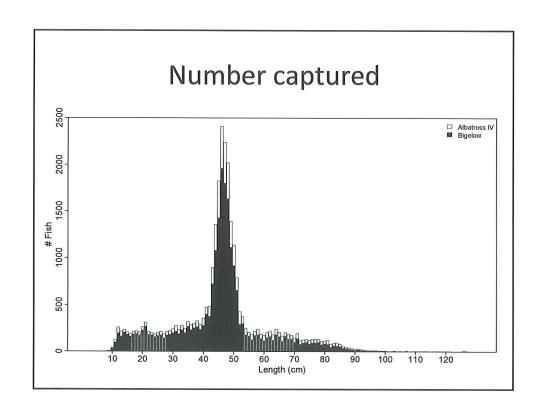
#### Determining a final Model 2 and 3

- The suite of fitted models with different smoothers types and numbers of parameters were compared using AIC<sub>c</sub> to determine a final Model 2.
- The same type of smoother as the final Model 2 was used for fitting models by season and region.
- Used AIC<sub>c</sub> to compare the fitted seasonal and regional models to each other and Model 2

#### **Calibration Data**

- For Model 1 (CRD 10-05), the data are numbers per tow for each vessel by species
- For Models 2 and 3 data are numbers per tow per 1 cm length class of all species combined.
- After preliminary analyses for Model 2 the PDT decided to pool information for skates greater than 94 cm.
  - Assigned 107 cm (average of lengths in this pool).



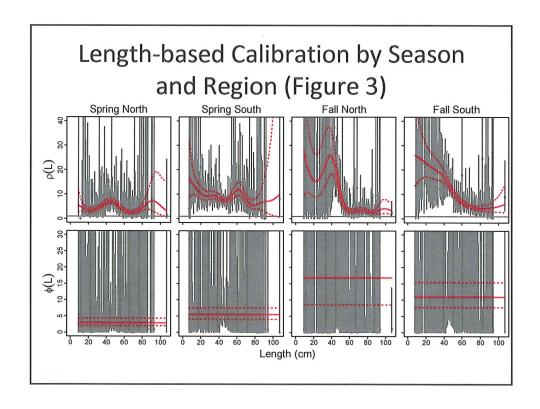


### Model 1 Results (Table 1)

| Calibration Coefficient (Std Err) | Comment   |
|-----------------------------------|---|
| 2.785519 (0.32)                   | Spring Survey   |
| 2.174334 (0.31)                   | Fall Survey   |
| 3.661128 (0.51)                   | Fall Survey   |
| 3.626359 (0.58)                   | Fall Survey   |
| 4.449518 (0.67)                   | Fall Survey   |
| 6.189401 (0.81)                   | Fall Survey   |
| 8.813973 (0.98)                   | Based on the calibration<br>coefficient for little skate<br>in the fall survey<br>comparisons |
|                                   | 2.174334 (0.31)<br>3.661128 (0.51)<br>3.626359 (0.58)<br>4.449518 (0.67)                      |

## Comparison of Models in classes 2 and 3(Table 6)

| Ran<br>k | Model Type     | #pdf  | # φ length<br>parameters | φ<br>Covariat<br>es | # Total parameters | -LL      | AIC <sub>c</sub> | (AIC <sub>c</sub> ) |
|----------|----------------|-------|--------------------------|---------------------|--------------------|----------|------------------|---------------------|
| 1        | SP(Season,Regi |       |                          | SF                  |                    |          |                  |                     |
|          | on)            | 37.02 | 5                        |                     | 46.02              | -7359.32 | 14811.18         | 0.00                |
| 2        | SP(Season)     | 15.56 | 4                        | SF                  | 23.56              | -7423.64 | 14894.53         | 83.36               |
| 3        | SP             | 6.80  | 1                        | SF                  | 8.80               | -7522.98 | 15063.58         | 252.40              |
| 4        | OP             | 9     | 1                        | SF                  | 11                 | -7520.85 | 15063.73         | 252.55              |
| 5        | OP             | 10    | 1                        | SF                  | 12                 | -7520.35 | 15064.74         | 253.57              |
| 6        | OP             | 9     | 2                        | SF                  | 12                 | -7520.49 | 15065.01         | 253.83              |
| 7        | SP             | 6.54  | 10.24                    | SF                  | 16.78              | -7515.75 | 15065.14         | 253.96              |
| 8        | SP             | 6.81  | 1                        | SF, SA              | 9.81               | -7522.88 | 15065.42         | 254.24              |
| 9        | OP             | 9     | 1                        | SF, SA              | 12                 | -7520.76 | 15065.56         | 254.38              |
| 10       | OP             | 10    | 2                        | SF                  | 13                 | -7520.00 | 15066.04         | 254.87              |
| 11       | OP             | 9     | 7                        | SF                  | 17                 | -7516.00 | 15066.07         | 254.90              |
| 12       | OP             | 11    | 1                        | SF                  | 13                 | -7520.24 | 15066.51         | 255.34              |



### Issues with converting previous Albatross indices into Bigelow Equivalents

- Potential biases due to changes in length composition if length-based methods not used
- Potential biases if length-weight relationships vary over time and data are not available to estimate them
- Re-calculation of reference points required
- Poorer precision of indices induced by conversion may translate into greater CVs in reference point algorithm
- Biases of conversion when zeros observed by Albatross (e.g., barndoor)
- All of this would imply the peer-review process would be appropriate for this change in reference point methodology